

**Personal Futures**

**Mathematics**

**Essential Mathematics 1**  
COURSE DOCUMENT

**PHASE 4**  
DRAFT FOR  
CONSULTATION



Catholic  
Education  
Tasmania



INDEPENDENT  
SCHOOLS  
TASMANIA

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## Essential Mathematics 150 hours – Level 1

This course is the Level 1 component of the proposed *Essential Mathematics* suite.

### Focus Area – Personal Futures

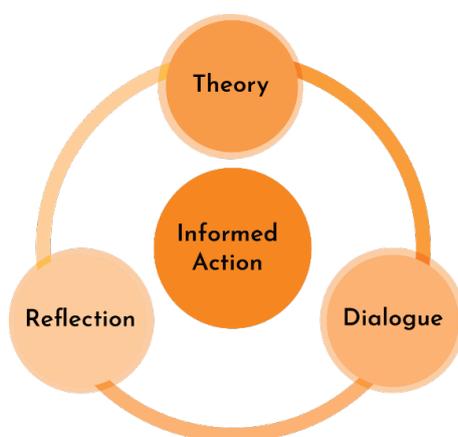
Courses aligned to the [Years 9 to 12 Curriculum Framework](#) belong to one of the five focus areas of Discipline-based Study, Transdisciplinary Projects, Professional Studies, Work-based Learning and Personal Futures.

*Essential Mathematics* Level 1 is a Personal Futures course.

Personal Futures courses prepare students to be independent young adults, able to lead healthy, fulfilled and balanced lives. Learning is highly personalised. Students develop strategies to optimise learning, make decisions, solve problems, set career and life goals, and pursue areas of strong personal interest. Personal Futures supports students to develop the required knowledge, skills and understandings to make informed choices that enhance their own and others' health and wellbeing. The inclusion of Personal Futures as a focus area responds to a range of contemporary research findings highlighting the importance of students having broad educational goals that include individual and collective wellbeing and opportunities for student agency as they navigate a complex and uncertain world.

Personal Futures courses have three key features that guide teaching and learning

- theory and dialogue
- informed action
- reflection and dialogue.



In this course learners will do this by:

- building foundational understanding, background knowledge, rules and conventions of mathematics
- interacting and working with other people, engaging in mathematical discourse to explore ideas, reasoning and approaches
- identifying challenges and problems, using problem-solving and mathematical reasoning to trial strategies, compare solutions, generate knowledge and take informed action
- reflecting on their own understanding, integrating prior knowledge and sharing solutions with others.

## Rationale

The *Essential Mathematics* Level 1 course is designed to develop adolescent learners' confidence and self-esteem to engage with mathematics and develop their ability to apply mathematical thinking and reasoning in real world contexts. In doing so, the course enables learners to build the requisite knowledge and skills and the capacity, confidence and disposition to use mathematics to take informed action in varied personal contexts.

This course will promote Mathematics and numeracy learning opportunities that aims to:

- enable learners to interpret everyday practical situations
- provide the basis for many informed personal decisions.

These aims will be met by developing learners' ability to formulate situations mathematically and to employ mathematical concepts, facts, procedures and reasoning to interpret these situations. This is more pertinent than ever before as 75% of the fastest growing occupations require competence in STEM with an estimated 44% or 5.1 million jobs in Australia at risk of digital disruption<sup>1</sup>. Successful completion of the course will provide learners with a level of mathematical competence that will enable them to contribute productively in the rapidly changing workforce.

The purpose of Years 9 to 12 Education is to enable all students to achieve their potential through Years 9 to 12 and beyond in further study, training or employment.

Years 9 to 12 Education enables Personal Empowerment, Cultural Transmission, Preparation for Citizenship and Preparation for Work.

This course is built on the principles of: Access, Agency, Excellence, Balance, Support and Achievement as part of a range of programs that enables students to access a diverse and flexible range of learning opportunities suited to their level of readiness, interests and aspirations.

Reference:

<sup>1</sup>Price-Waterhouse Report (April, 2015). A Smart Move: Future proofing Australia's workforce by growing skills in science, mathematics, engineering and maths (STEM)

## Learning Outcomes

On successful completion of this course learners will be able to:

1. communicate thinking, strategies and solutions using appropriate mathematical or statistical language
2. plan, organise and manage learning to complete tasks and assess progress
3. understand concepts and apply numeric techniques and multiplicative thinking to represent situations and solve problems
4. apply mathematical reasoning to make inferences, generalise and represent relationships and explain thinking in a range of contexts
5. act as creative, critical and reflective thinkers to assess ideas and take informed action
6. understand concepts and apply techniques to solve problems and make informed choices in situations involving pattern and algebra
7. understand concepts and apply techniques to solve problems and make informed choices in situations involving statistics and probability
8. understand concepts and apply techniques to solve problems and make informed choices in situations involving measurement and geometry

## Integration of General Capabilities and Cross-Curriculum Priorities

The general capabilities addressed specifically in this course are:

- Critical and creative thinking 
- Literacy 
- Numeracy 
- Personal and social capability 

The cross-curriculum priorities which may be enabled through this course are:

- Aboriginal and Torres Strait Islander Histories and Cultures 
- Sustainability 

## Course Description

*Essential Mathematics* Level 1 is designed to build foundational knowledge of mathematics that enables learners to select and apply problem-solving strategies and mathematical techniques to engage in situations involving:

- number, proportional reasoning, financial mathematics and pattern
- using units of measurement, shape, maps and plans
- everyday chance events, data collection and representation.

Learners will develop their multiplicative thinking and mathematical reasoning by:

- engaging in mathematical discussions
- working on collaborative problem-solving tasks
- sharing strategies and solutions
- providing explanations for their answers.

They will reflect on everyday scenarios involving mathematics and will integrate their prior knowledge, skills, attitudes and values in mathematics to refine and improve their understanding and personal decisions.

## Pathways

The *Essential Mathematics* Level 1 course enables learning continuity from Year 10 Australian Curriculum Mathematics for learners who have attained either a 'D' or 'E' rating or alternatively in earlier years for learners where an agreed Individual Education Plan is in place.

*Essential Mathematics* Level 1 will provide the fundamental knowledge for learners pursuing further mathematics study in *Essential Mathematics* Level 2A and *Essential Mathematics* Level 2B.

## Course Requirements

### Access

This course requires learners to collaborate with others.

### Resource Requirements

The learning outcomes in this course require learners to have access to specific mathematics manipulatives and concrete materials including counters, dice, spinners, blocks, 3-Dimensional models.

Learners will require access to general calculators in this course. On occasions, computers and the internet will be required to enable learners' access to information and data sources.

## Course Structure and Delivery

### Structure

This course consists of three 50-hour modules.

#### Modules Available

- Module 1: Pattern and algebraic reasoning
- Module 2: Probability and statistical reasoning
- Module 3: Measurement and geometric reasoning

### Delivery

Module 1 should be delivered first, or concurrently with Module 2 and Module 3 which can be taught in any order.

### Module 1 – Pattern and algebraic reasoning

This module contains three topics:

- Number and place value
- Fractions, decimals and percentages
- Algebraic reasoning

'Number and place value' and 'Fractions, decimals and percentages' will enable learners to develop a capacity to work flexibly and efficiently with whole numbers, decimals, common fractions, rates and percentages. In turn this will improve learners' ability to recognise and solve problems involving multiplication and division including direct and indirect proportion. These skills will provide the foundation upon which learners will apply to the remaining course content.

'Algebraic reasoning' will enable learners to develop the capacity to communicate mathematical situations effectively through words, symbolic expressions, written algorithms and other representations. They will explore, describe and extend number patterns, find generalisations in situations involving two variables, identify equivalent expressions and explore equivalence, factors and properties of numbers.

### Module 1 Learning Outcomes

On successful completion of this module, learners will be able to:

1. communicate thinking, strategies and solutions using appropriate mathematical or statistical language
2. plan, organise and manage learning to complete tasks and assess progress
3. understand concepts and apply numeric techniques and multiplicative thinking to represent situations and solve problems
4. apply mathematical reasoning to make inferences, generalise and represent relationships and explain thinking in a range of contexts
5. act as creative, critical and reflective thinkers to assess ideas and take informed action
6. understand concepts and apply techniques to solve problems and make informed choices in situations involving pattern and algebra

## Module I Content

### Key knowledge and skills

#### Topic 1. Number and place value:

- Investigate and use the properties of odd and even numbers
- Identify and describe factors and multiples of whole numbers and use them to solve problems
- Solve problems involving multiplication of large numbers by one- or two-digit numbers using efficient mental, written strategies and appropriate digital technologies
- Investigate everyday situations that use integers. Locate and represent these numbers on a number line
- Compare, order, add and subtract integers
- Carry out the four operations with integers, using efficient mental and written strategies and appropriate digital technologies
- Apply place value to partition, rearrange and regroup numbers to at least ten thousand to assist calculations and solve problems
- Make connections between fractions and decimal notation
- Recognise that the place value system can be extended beyond hundredths
- Solve problems involving division by a one-digit number, including those that result in a remainder
- Use estimation and rounding to check the reasonableness of answers to calculations
- Select and apply efficient mental and written strategies and appropriate digital technologies to solve problems involving all four operations with whole numbers eg choose to calculate  $5 \times 12$  rather than  $12 + 12 + 12 + 12 + 12$  to answer the question if I buy 5 cartons of 12 eggs how many eggs do I have?
- Recognise and use the correct order of operations for a multi-step equation, for example:
  - Complete the division first in the equation  $18 \div 6 - 2$
- Apply the associative, commutative and distributive laws to aid mental and written computation
- Calculate to make comparisons between items, for example:
  - Multiply the cost of a 500 gram bag of flour  $\times 4$  to compare it to the price of a 2kg bag of flour
- Use a calculator to assist in solving multi-step number problems involving large numbers, for example:
  - A stall at the athletics carnival is selling sausages for \$1.50. If the stall buys six  $\times$  20 packs of sausages for \$12 each and 4 loaves of bread (30 slices) for \$4.50 each, how many sausages would the stall need to sell to start making a profit?

#### Topic 2. Fractions, decimals and percentages:

- Count by quarters, halves and thirds, including with mixed numerals. Locate and represent these fractions on a number line
- Compare fractions with related denominators and locate and represent them on a number line
- Investigate strategies to solve problems involving addition and subtraction of fractions with the same denominator
- Compare fractions using equivalence. Locate and represent positive and negative fractions and mixed numbers on a number line
- Solve problems involving addition and subtraction of fractions, including those with unrelated denominators
- Find a simple fraction of a quantity where the result is a whole number, with and without the use of digital technologies

- Express one quantity as a fraction of another, with and without the use of digital technologies
- Compare, order and represent decimals
- Investigate terminating and recurring decimals
- Round decimals to a specified number of decimal places
- Multiply and divide decimals by powers of 10
- Connect fractions, decimals and percentages and carry out simple conversions
- Find percentages of quantities and express one quantity as a percentage of another, with and without the use of digital technologies
- Solve problems involving the use of percentages, including percentage increases and decreases, with and without the use of digital technologies
- Estimate costs and change on purchases, for example:
  - Select appropriate coins and notes to cover the cost of purchases
  - Use rounding to an appropriate nomination to estimate the amount of change due on purchases for example, large appliances to the nearest \$100, groceries to the nearest dollar or nearest \$10 for bulk items etc
- Solve problems involving purchases and the calculation of change due using a range of strategies, including concrete materials, mental, written and calculator techniques as appropriate
- Interpret the use of percentages in everyday life, for example:
  - Investigate and calculate percentage discounts of 10%, 25% and 50% on sale items, with and without the use of digital technologies

### Topic 3. Algebraic reasoning

This topic has two subtopics:

- Rates, ratio and proportion
- Pattern, modelling and equivalence

#### *Rates, ratio and proportion:*

- Use and apply rates and ratios and their units in familiar situations, for example:
  - Speed (km/hr), ingredient costs (\$/kg), mixing quantities (1 part: 5 parts)
- Compare familiar rates and ratios, and describe difference using simple language, for example:
  - Which is faster?
  - Which is a stronger mix of cordial?
- Recognise and describe proportional growth in real terms in familiar situations, for example:
  - A puppy weighed 2 kg when it was born. At six months its weight had tripled. How much does the puppy weigh?

#### *Pattern, modelling and equivalence:*

- Explore and describe number patterns resulting from performing multiplication
- Describe, continue and create patterns with familiar fractions, decimals and whole numbers resulting from addition and subtraction
- Solve word problems by using number sentences involving multiplication or division where there is no remainder
- Find unknown quantities in number sentences involving multiplication and division and identify equivalent number sentences involving multiplication and division
- Introduce the concept of symbols as a way of representing numbers using letters

- Investigate and use square roots of perfect square numbers
- Model real-life problems using concrete materials and/or diagrams, for example:
  - Find the number of people that can be seated in a classroom by setting up different configurations of tables and chairs, or by drawing a diagram
- Complete a table of values to describe modelled situations
- Generalise a rule based on modelled real-life problems and use to create solutions, for example:
  - When configuring the classroom with rectangular tables individually it can seat 2 people on each long end and 1 person on each short end. In this configuration, the number of chairs needed for any number of tables is number of chairs = number of tables  $\times$  6
  - When two or more of these tables are joined together at the long end the number of chairs needed = (number of tables  $\times$  2) + 4

### Module 1 Work Requirements Summary

The work requirements of a course are processes, products or performances that provide a significant demonstration of achievement that is measurable against the course's standards. Work requirements need not be the sole form of assessment for a module.

This module includes 10 short responses as work requirements.

See Appendix 3 for summary of Work Requirement specifications for this course.

### Module 1 Assessment

This module has a focus on criteria 1, 2, 3, 4, 5 and 6.

### Module 2 – Probability and statistical reasoning

This module contains two topics:

- Chance
- Data collection, representation and interpretation

'Chance' provides an opportunity for learners to describe the probability of everyday events occurring, to construct and carry out single-step experiments for equiprobable outcomes. Learners will use mathematical reasoning to compare the frequency of outcomes with theoretical probability equating differences to concepts including randomness, variation and distribution.

'Data collection, representation and interpretation' enables learners to select and trial simple data collection processes and to represent, read and interpret information in routine tables, graphs and charts including column graphs, picture graphs, dot plots and stem-and-leaf plots. They will explore the variation between different samples taken from the same population and investigate the effect of individual data values on the mean and median.

### Module 2 Learning Outcomes

On successful completion of this course learners will be able to:

1. communicate thinking, strategies and solutions using appropriate mathematical or statistical language
2. plan, organise and manage learning to complete tasks and assess progress
3. understand concepts and apply numeric techniques and multiplicative thinking to represent situations and solve problems
4. apply mathematical reasoning to make inferences, generalise and represent relationships and explain thinking in a range of contexts

5. act as creative, critical and reflective thinkers to assess ideas and take informed action
7. understand concepts and apply techniques to solve problems and make informed choices in situations involving statistics and probability

## Module 2 Content

### *Key knowledge and skills:*

#### Topic 1. Chance:

- Describe possible everyday events and order their chances of occurring
- Identify everyday events where one cannot happen if the other happens
- Identify events where the chance of one will not be affected by the occurrence of the other
- Recognise that probabilities range from 0 (impossible) to 1 (certain)
- Represent probabilities using a range of notations, for example:
  - Words
  - Fractions
  - Ratios
  - Percentages
- List outcomes of chance experiments involving equally likely outcomes and represent probabilities of those outcomes using fractions
- Construct sample spaces for single-step experiments with equally likely outcomes
- Describe probabilities using fractions, decimals and percentages
- Assign probabilities to the outcomes of events and determine probabilities for events
- Conduct chance experiments with both small and large numbers of trials using appropriate digital technologies
- Identify possible reasons for variations and distribution of outcomes in trials
- Compare the likelihood of events based on their numerical probability
- Compare observed frequencies across experiments with expected frequencies
- Draw conclusions or make predictions from the results of probability experiments

#### Topic 2. Data collection, representation and interpretation:

- Select and trial methods for data collection, including survey questions and recording sheets
- Pose questions and collect categorical or numerical data by observation or survey
- Identify the key features of graphs and data displays, including heading, scale, key, axes and labels
- Construct simple graphs, from given or collected data using provided scales and axes with gradations of 1s, 5s, 10s or 100s, including column graphs and dot plots
- Construct tables, and picture graphs where one picture can represent many data values
- Construct frequency tables and make calculations related to these, for example:
  - Calculate the total for each column
- Construct and compare a range of data displays including stem-and-leaf plots and dot plots
- Interpret and compare a range of data displays, including side-by-side column graphs for two categorical variables
- Assess the accuracy and fairness of a graph, for example:
  - Check it has all the necessary key features
  - Check if it has any misleading information
- Recognise that the terms 'mean' and 'average' describe the same concept in everyday use, for example:
  - Cricket batting or bowling averages

- Calculate mean, median, mode and range for sets of simple data. Interpret these statistics in the context of data
- Describe and interpret data displays using median, mean and range
- Identify variability and randomness in experimental data eg a 6-sided die is rolled 30 times (expected results 5 rolls of each number versus actual results)
- Identify and describe variability or randomness in data displays

### Module 2 Work Requirements Summary

The work requirements of a course are processes, products or performances that provide a significant demonstration of achievement that is measurable against the course's standards. Work requirements need not be the sole form of assessment for a module.

This module includes one (1) project as work requirements.

See Appendix 3 for summary of Work Requirement specifications for this course.

### Module 2 Assessment

This module has a focus on criteria 1, 2, 3, 4, 5 and 7.

### Module 3 – Measurement and geometric reasoning

This module contains three topics:

- Using units of measurement
- Shapes, maps and plans
- Geometric reasoning

'Using units of measurement' enables learners to perform measurements using scaled instruments, connect decimal representations to the metric system and name, convert and use appropriate units of measure. They will estimate, calculate and solve problems involving length, area, volume and capacity, temperature and time.

'Shapes, maps and plans' will enable learners to develop their knowledge of 2-Dimensional shapes and 3-Dimensional objects. They will utilise this knowledge of the attributes and properties of shapes to construct, compare, draw and describe objects. Learners will use the features of routine maps, plans and timetables to read and interpret information, describe locations and routes and calculate distances or travel time.

'Geometric reasoning' will enable learners to describe translations, reflections and rotations of shapes, identify line and rotational symmetry and create symmetrical patterns and pictures. Learners will measure, construct and classify angles and use their properties to classify triangles, describe quadrilaterals and investigate relationships between angles.

### Module 3 Learning Outcomes

On successful completion of this course learners will be able to:

1. communicate thinking, strategies and solutions using appropriate mathematical or statistical language
2. plan, organise and manage learning to complete tasks and assess progress
3. understand concepts and apply numeric techniques and multiplicative thinking to represent situations and solve problems
4. apply mathematical reasoning to make inferences, generalise and represent relationships and explain thinking in a range of contexts

5. act as creative, critical and reflective thinkers to assess ideas and take informed action
8. understand concepts and apply techniques to solve problems and make informed choices in situations involving measurement and geometry

## Module 3 Content

### *Key knowledge and skills:*

#### Topic 1. Using units of measurement:

- Estimate and compare lengths, masses and capacities, for example:
  - Decide if the food in one container will fit into another container of a different shape
  - The different masses of items to be packed into hand luggage and suitcases so that maximum limits are not exceeded
- Use scaled instruments to measure and compare lengths, masses, capacities, time and temperatures
- Use comparative language that relates to length, time, temperature, mass, capacity and volume
- Calculate perimeters by adding given side lengths from diagrammatic representations of shapes
- Solve problems involving perimeter, for example:
  - Calculate how much barricade tape is required to cordon off the cricket pitch area of the school oval
- Calculate the perimeter and area of rectangles and triangles using familiar metric units
- Connect decimal representations to the metric system
- Recognise and use metric units of length, area, volume, capacity and mass, and their abbreviations
- Convert between common metric units of length, mass and capacity
- Recognise the unit °Celsius and its abbreviation °C
- Solve problems involving the comparison of lengths and areas using appropriate units
- Investigate the relationship between mass, volume and capacity and their units of measurement
  - Discover and apply the fact that 1 L of water weighs 1 kg
  - Discover and use the fact that 1 mL of water is equivalent to 1 cm<sup>3</sup>
  - Recognise that large objects can be very light, while smaller objects can be very heavy
- Tells time using analogue and digital clocks using a 12-hour time system
- Interpret calendars and calculate days between dates
- Use 'am' and 'pm' notation and solve simple time problems
- Convert between units of time
- Compare 12- and 24-hour time systems and convert between them

#### Topic 2. Shapes, maps and plans:

- Compare the areas of regular and irregular shapes by informal means
- Compare and describe two-dimensional shapes that result from combining and splitting common shapes, with and without the use of digital technologies
- Connect three-dimensional objects with their nets and other two-dimensional representations
- Construct simple prisms and pyramids
- Draw different views of prisms and solids formed from combinations of prisms
- Solve problems involving two-dimensional shapes and three-dimensional objects, for example:
  - Construct a two-dimensional net that will produce a three-dimensional package of 6 golf balls
  - Position net templates on an A3 card to use the card as sustainably as possible

- Use simple scales, legends and directions to locate positions or gather information contained in basic maps
- Use a simple grid reference system to describe locations. Describe routes using landmarks and directional language
- Use the Cartesian coordinate system:
  - Initially using the top right quadrant
  - Introducing the bottom right quadrant in situations such as above and below sea level
  - Introducing the top left quadrant in situations involving movement either side of a fixed origin
- Create simple maps, for example:
  - Sketch a map to show how to get from one location to another
- Solve problems involving maps, for example:
  - Identify or calculate travel time and distance between two places using given information
  - Determine estimated time of arrival based on given distance and other parameters based on experience (such as traffic at time of travel, reliability of public transport etc)
- Use plans to locate positions or gather information, for example:
  - Interpret a site plan of a local market
  - Use a plan of a stadium to find their allocated seat
- Construct simple plans, for example:
  - Complete a floor plan of their home or a shopping centre
- Investigate travel times using digital technology, for example:
  - Public transport planning websites or apps
- Use and interpret time to plan travel, for example:
  - Use calendars to consider travel dates
  - Identify the typical features of each season and use this to make decisions about recreation activities and clothing required
- Read and interpret timetables in a range of formats and contexts, for example:
  - Everyday timetables, such as school, cinema, local fitness centre, TV guide
  - Travel timetables, such as bus, ferry, flight
  - Event timetables, such as a sporting competition or a festival program
- Solve everyday problems involving time, for example:
  - Is there enough time to walk to the cinema before the movie starts?
  - Identify what time to leave home to arrive somewhere by a given time if getting a lift or travelling on public transport

### Topic 3. Geometric reasoning:

- Estimate, measure and compare angles using degrees. Construct angles using a protractor
- Compare angles and classify them by name according to angle size (acute, obtuse, right, straight, reflex and rotation)
- Classify triangles according to their side and angle properties
- Investigate angles on a straight line, angles at a point and vertically opposite angles. Use results to find unknown angles
- Demonstrate that the angle sum of a triangle is  $180^\circ$  and use this to find the angle sum of a quadrilateral

- Describe translations, reflections and rotations of two-dimensional shapes. Identify line and rotational symmetries
- Create symmetrical patterns, pictures and shapes

### Module 3 Work Requirements Summary

The work requirements of a course are processes, products or performances that provide a significant demonstration of achievement that is measurable against the course's standards. Work requirements need not be the sole form of assessment for a module.

This module includes 10 short responses as work requirements.

See Appendix 3 for summary of Work Requirement specifications for this course.

### Module 3 Assessment

This module has a focus on criteria 1, 2, 3, 4, 5 and 8.

## Assessment

Criterion-based assessment is a form of outcomes assessment that identifies the extent of learner achievement at an appropriate end-point of study. Although assessment – as part of the learning program – is continuous, much of it is formative, and is done to help learners identify what they need to do to attain the maximum benefit from their study of the course. Therefore, assessment for summative reporting to TASC will focus on what both teacher and learner understand to reflect end-point achievement.

The standard of achievement each learner attains on each criterion is recorded as a rating 'A', 'B', or 'C', according to the outcomes specified in the standards section of the course.

A 't' notation must be used where a learner demonstrates any achievement against a criterion less than the standard specified for the 'C' rating.

A 'z' notation is to be used where a learner provides no evidence of achievement at all.

Internal assessment of all criteria will be made by the provider. Providers will report the learner's rating for each criterion to TASC.

### Criteria

	Module 1	Module 2	Module 3
Criteria Assessed	1,2,3,4,5,6	1,2,3,4,5,7	1,2,3,4,5,8

The assessment for *Essential Mathematics* Level 1 will be based on the degree to which the learner can:

1. interpret and communicate mathematical information and ideas and apply mathematical conventions in a range of contexts
2. manage and take responsibility for learning and assess mathematical development
3. interpret concepts and apply numeric techniques and multiplicative thinking to represent real-world situations and solve problems
4. apply mathematical reasoning to make inferences, generalise and represent relationships and explain thinking in a range of contexts

5. create, apply and reflect on mathematical strategies to solve problems, refine personal decisions and take informed action
6. interpret concepts and apply mathematical techniques to solve and make informed choices in situations involving pattern and algebra
7. interpret concepts and apply mathematical techniques to solve problems and make informed choices in situations involving probability and statistics
8. interpret concepts and apply mathematical techniques to solve problems and make informed choices in situations involving measurement and geometry

## Standards

Criterion 1: interpret and communicate mathematical information and ideas and apply mathematical conventions in a range of contexts

Standard Element	Rating C	Rating B	Rating A
E1 – interprets information	interprets mathematical information and ideas in routine texts in familiar and personally relevant contexts	interprets and sequences mathematical information and ideas in routine texts in familiar contexts	interprets, sequences and abstracts embedded mathematical information and ideas from routine texts in familiar contexts
E2 – describe mathematical situations	recalls and uses some mathematical facts, rules and definitions to describe mathematical situations	selects, recalls and uses some mathematical facts, rules and definitions to describe mathematical situations	consistently selects, recalls and uses mathematical facts, rules, definitions and procedures correctly to describe mathematical situations
E3 – uses conventions	uses a combination of formal and informal mathematical conventions and informal symbolism	uses formal mathematical conventions, including formal symbolic expressions and rules appropriately on most occasions	uses mathematical conventions and systems including formal symbolic expressions accurately and purposefully
E4 - expresses ideas	selects and uses language to express ideas and recalls the ideas of others	selects, uses and refines language to respond to multiple ideas	purposefully selects, uses and refines language to effectively respond to multiple ideas
E5 – identifies solutions	presents work with the final answer apparent.	presents work with the final answer clearly identified.	presents work with the final answer clearly identified and articulated in terms of the question where necessary.

Criterion 2: manage and take responsibility for learning and assess mathematical development

Standard Element	Rating C	Rating B	Rating A
E1 – self-awareness	identifies some learning strengths and weaknesses with support <sup>†</sup>	identifies personal traits that promote and inhibit learning performance and understanding	recognises own learning strengths and weaknesses and establishes processes to plan, monitor and assess understanding and performance
E2 – time management	identifies a goal with support <sup>†</sup> for individual learning activities, and recalls when prompted	sets goals and timelines and assesses progress with support <sup>†</sup>	sets goals and timelines and assesses progress
E3 – planning and organisation	follows given planning strategies to complete set tasks with support <sup>†</sup>	organises and plans with support <sup>†</sup> in order to manage resources and complete set tasks	displays organisational, planning and self-management skills to manage resources and consistently complete tasks
E4 - collaboration	identifies tasks to be completed in individual and collaborative activities with support <sup>†</sup>	identifies tasks to be completed in individual and collaborative activities	performs tasks as directed to contribute to the completion of individual and collaborative activities
E5 – self-monitoring	identifies own contribution in collaborative activities.	describes own contribution in collaborative activities.	describes how own contributions assisted in the completion of collaborative activities.

<sup>†</sup>support in this course refers to allowing the student to work alongside a teacher / mentor / aide. This person will differentiate the level of support required to support the student, for example: prompt the student to identify planning strategies, recall their input to a group task, identify a goal on a learning activity.

Criterion 3: interpret concepts and apply numeric techniques and multiplicative thinking to represent real-world situations and solve problems

Standard Element	Rating C	Rating B	Rating A
E1 - uses properties of numbers	identifies odd and even numbers and explains if an integer is divisible by two with or without remainder and can find multiples as an application of repeated addition	identifies factors of whole numbers up to 100 using divisibility of the number by 2, 3, 4, 5 and 10 and multiples using mental and written computation strategies including arrays	identifies all factors of whole numbers up to 100 using divisibility rules and solves problems involving multiples using efficient mental, written strategies and appropriate digital technologies
E2 – applies order of operations	applies order of operations to solve calculations involving whole numbers	applies order of operations to solve multi-step calculations involving whole numbers, routine fractions, decimals and percentages	applies order of operations to solve multi-step calculations involving integers, fractions, decimals and percentages and flexibly uses equivalent forms
E3 – uses equivalent representations	orders whole numbers, routine fractions, decimals and percentages	compares and orders whole numbers, routine fractions, decimals and percentages, and converts between different forms	flexibly uses equivalent representations of numbers to solve problems in context
E4 – applies place value	makes, compares, orders, sequences and counts forwards and backwards in place-value parts, numbers involving decimal fractions of tenths and hundredths.	applies place value to partition, rearrange, regroup and rename numbers to at least 10000 and decimal fractions to tenths.	applies place value to partition, rearrange, regroup and rename numbers to at least 10000 and decimal fractions to hundredths including situations involving money.

Criterion 4: apply mathematical reasoning to make inferences, generalise and represent relationships and explain thinking in a range of contexts

Standard Element	Rating C	Rating B	Rating A
E1 – makes inferences	makes observations and responds to patterns or data sets	makes inferences that may be able to be tested mathematically	makes informed inferences that can be tested mathematically
E2 – generalises relationships	identifies and describes simple arithmetic relationships that can be generalised using a rule	explores and makes predictions about patterns and identifies generalisations based on known information	explains generalisations by telling number stories in words, with materials and using symbols
E3 – explains thinking about mathematical techniques	identifies the mathematical techniques used in calculations.	describes and explains how the mathematical techniques were used.	explains why the mathematical techniques used were appropriate for the context.

Criterion 5: create, apply and reflect on mathematical strategies to solve problems, refine personal decisions and take informed action

Standard Element	Rating C	Rating B	Rating A
E1 – creates mathematical strategies	with support, generates ideas and approaches to solve problems	generates ideas and approaches to solve problems	generates ideas and refines chosen approaches to solve problems
E2 – reflects and builds understanding	uses reflective thinking strategies to recall what they know from prior learning	uses reflective thinking strategies to recall what they learned in a mathematical situation	uses reflective thinking strategies to describe their own understanding of a situation in mathematical terms
E3 – checks solutions	uses a given method of solution and checks solution against given answer	chooses and applies an appropriate method of solution from a limited range of mathematical processes and checks outcomes using a given method	selects and applies mathematical and problem-solving strategies purposefully and checks outcomes using alternative methods
E4 – refines personal thinking	identifies when their thinking has changed	describes how their thinking has changed	explains why their thinking has changed over time

Standard Element	Rating C	Rating B	Rating A
E5 – plans and takes informed action	with support, plans and takes action in a given context.	plans and takes action in a given context.	plans and takes informed action in given contexts.

Criterion 6: interpret concepts and apply mathematical techniques to solve and make informed choices in situations involving pattern and algebra

Standard Element	Rating C	Rating B	Rating A
E1 – explores patterns	explores and describes number patterns resulting from performing addition or multiplication using whole numbers or routine fractions	describes, continues and creates patterns with fractions, decimals and whole numbers using any of the four standard operations <sup>†</sup>	solves word problems by creating number sentences and interpreting pattern using any of the four standard operations <sup>†</sup>
E2 – use rates and ratios	uses and applies rates in familiar and personally relevant situations eg km/hr, bpm, unit-costs	uses and applies rates and ratios in familiar and personally relevant situations eg km/hr, m/s mixing quantities, scaling recipes, and compares differences using simple language	uses and applies rates and ratios in familiar situations including making conversions eg km/hr to m/s, and compares differences by calculation
E3 – maintains equivalence	represents the same pattern or solution to a problem in different but equivalent ways.	maintains equivalence between two amounts using relational thinking and examines the relationships between different factors that when multiplied give the same result.	explores the relationships of two numbers or quantities as they vary simultaneously as equivalent expressions and explains why they are equivalent.

<sup>†</sup> the four standard operations are addition, subtraction, multiplication and division (without remainder)

Criterion 7: interpret concepts and apply mathematical techniques to solve problems and make informed choices in situations involving probability and statistics

Standard Element	Rating C	Rating B	Rating A
E1 – collects data	applies a familiar data collection process to collect information to answer a simple statistical question	selects and applies a familiar data collection process to collect numerical or categorical information to answer a simple statistical question	selects and applies a data collection process to collect numerical and/or categorical data to answer a statistical question involving two variables
E2 – organises data	organises familiar and personally relevant data and constructs tables, graphs and charts using given scales and axes	organises numerical or categorical information and represents in familiar tabular and/or graphical formats using chosen scales and axes	represents numerical and/or categorical information purposefully and accurately in tabular and graphical formats using appropriate scales and axes
E3 – interprets data	accurately reads information represented in simple tables, graphs and charts including comparison between categories or individual results and identifying median, mode and/or range	interprets information represented in simple tables, graphs and charts including identifying likelihood of chance events based on experimental data, and calculating mean, median mode and/or range	interprets information represented in tables, graphs and charts and performs calculations to compare averages between different data sets
E4 – describes chance	describes and compares the likelihood of everyday chance events using qualitative terms including certain, likely, impossible and relates these to routine fractions, decimals or percentages.	describes, compares and interprets the likelihood of everyday chance events using qualitative terms on a decimal scale between 0 (impossible) and 1 (certain).	compares and describes theoretical and experimental probability of everyday events; identifies and explains variation, randomness and distribution of the data.

Criterion 8: interpret concepts and apply mathematical techniques to solve problems and make informed choices in situations involving measurement and geometry

Standard Element	Rating C	Rating B	Rating A
E1 – uses properties of shape	uses properties of 2-Dimensional shapes and 3-Dimensional objects to describe and draw everyday objects	identifies the shape and relative position of faces of 3-Dimensional objects to describe, draw and construct 3-Dimensional objects from nets or concrete materials	measures or calculates lengths and angles of each face of 3-Dimensional objects and accurately describes, draws or constructs scale models from nets or concrete materials
E2 – uses properties of angle	identifies and measures common angles using simple tools and estimates unknown angles	measures and compares angles between 0 and 180 degrees and classifies them as right, acute, obtuse, or straight	constructs angles accurately using a protractor and measures and classifies angles between 0 and 360 degrees
E3 – measures and converts	uses simple scaled instruments to measure and compare lengths, masses, capacity, time and temperature and estimates unknown measurements in familiar and personally relevant situations	uses scaled instruments appropriately to measure and compare lengths, masses, capacity, time and temperature and calculates perimeter and area of rectangles using familiar metric units	converts between time systems and routine metric units in situations involving length, mass, capacity and temperature, and estimates the area of 2-Dimensional shapes using informal means
E4 – uses maps and plans	uses distance, direction, co-ordinates, simple scales, labels, symbols and keys to read and use familiar and personally relevant maps and plans	uses a grid reference system to describe locations and create maps, and describes routes on familiar maps using landmarks, co-ordinates and directional language	uses, calculates and interprets information on familiar maps and plans including scales, compass points, travel distances, speeds and times to describe locations and routes
E5 – uses time and interprets timetables and calendars	tells analogue and digital time and identifies key information on familiar and personally relevant timetables and calendars.	relates analogue and digital time and day of week to information on familiar timetables and calendars.	calculates time periods and solves problems involving interpretation of familiar timetables and calendars.

## Quality Assurance

- This will be determined by TASC at time of accreditation.

## Qualifications and Award Requirements

### Level I

The final award will be determined by the Office of Tasmanian Assessment, Standards and Certification from 8 ratings.

The minimum requirements for an award are as follows:

#### EXCEPTIONAL ACHIEVEMENT (EA)

6 'A' ratings, 2 'B' ratings

#### HIGH ACHIEVEMENT (HA)

3 'A' ratings, 4 'B' ratings, 1 'C' rating

#### COMMENDABLE ACHIEVEMENT (CA)

4 'B' ratings, 3 'C' ratings

#### SATISFACTORY ACHIEVEMENT (SA)

6 'C' ratings

#### PRELIMINARY ACHIEVEMENT (PA)

4 'C' ratings

A learner who otherwise achieves the rating for a CA (Commendable Achievement) or SA (Satisfactory Achievement) award but who fails to show any evidence of achievement in one or more criteria ('z' notation) will be issued with a PA (Preliminary Achievement) award.

## Course Evaluation

- This will be confirmed by time of accreditation.

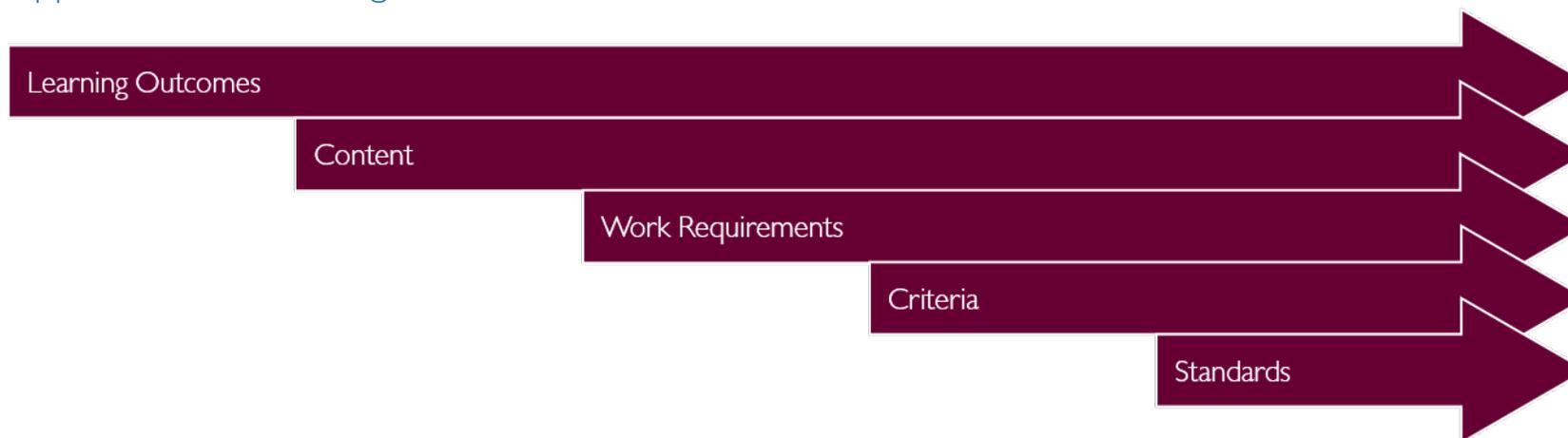
## Course Developer

This course has been developed by the Department of Education's Years 9 to 12 Learning Unit in collaboration with Catholic Education Tasmania and Independent Schools Tasmania.

## Accreditation and Version History

- Details to be determined by TASC at time of accreditation.

## Appendix I - Line of Sight



Learning Outcomes	Course Content	Work Requirements	Criteria	Standards	General Capabilities (GC)
1. communicate thinking, strategies and solutions using appropriate mathematical or statistical language	Module 1, 2, 3	Module 1, 2, 3	C 1	E 1, 2, 3, 4, 5	GC: 
2. plan, organise and manage learning to complete tasks and assess progress	Module 1, 2, 3	Module 1, 2, 3	C 2	E 1, 2, 3, 4, 5	GC: 
3. understand concepts and apply numeric techniques and multiplicative thinking to represent situations and solve problems	Module 1, 2, 3	Module 1, 2, 3	C 3	E 1, 2, 3, 4	GC: 
4. apply mathematical reasoning to make inferences, generalise and represent relationships and explain thinking in a range of contexts	Module 1, 2, 3	Module 1, 2, 3	C 4	E 1, 2, 3	GC: 

Learning Outcomes	Course Content	Work Requirements	Criteria	Standards	General Capabilities (GC)
5. act as creative, critical and reflective thinkers to assess ideas and take informed action	Module 1, 2, 3	Module 1, 2, 3	C 5	E 1, 2, 3, 4, 5	GC: 
6. understand concepts and apply techniques to solve problems and make informed choices in situations involving pattern and algebra	Module 1	Module 1	C 6	E 1, 2, 3	GC: 
7. understand concepts and apply techniques to solve problems and make informed choices in situations involving statistics and probability	Module 2	Module 2	C 7	E 1, 2, 3, 4	GC: 
8. understand concepts and apply techniques to solve problems and make informed choices in situations involving measurement and geometry	Module 3	Module 3	C 8	E 1, 2, 3, 4, 5	GC: 

## Appendix 2 - Alignment to Curriculum Frameworks

*Essential Mathematics* Level 1 aligns with course content contained in:

- Predominantly Level 2, and where deemed necessary to enable access, Level 1 of the Australian Core Skills Framework (ACSF).
- Australian Curriculum Mathematics.

## Appendix 3 - Work Requirements

### Module 1 Work Requirements Specifications

**Focus Area:** Personal Futures

**Title of Work Requirement:** Pattern and algebraic reasoning

**Mode /Format:** Folio of short responses (written question and answer / oral interview and mathematical calculations or manipulation of materials).

**Description:** Learners will complete a series of short responses where they will employ a range of mathematical techniques and procedures, problem solving strategies and mathematical reasoning to make informed choices relating to personal situations involving pattern and algebra.

Evidence of mathematical thinking and calculations can be captured through observation and/or recording of use of manipulatives and learner responses and discussion can be captured through written, oral or AAC methods as appropriate for the learner. Additionally, where possible, learners should be provided with opportunities to collaborate in pairs, or small groups and enabled to engage in mathematical discussion to share ideas, solutions and thinking.

**Size:** Between 6 and 10 responses equivalent to 2-3 written sentences each and associated mathematical calculations.

**Timing:** Ongoing throughout module.

**External agencies:** At teacher discretion.

**Relevant criteria:**

- Criterion 1: E1, E2, E3, E5 and where relevant E4
- Criterion 2: E1, E2, E3, E4 and E5 as appropriate
- Criterion 3: E1, E2 and where relevant E3
- Criterion 4: all elements
- Criterion 5: E1, E2, E3 and where relevant E4
- Criterion 6: all elements

### Module 2 Work Requirements Specifications

**Focus Area:** Personal Futures

**Title of Work Requirement:** Measurement and geometric reasoning

**Mode /Format:** Folio of short responses (written question and answer / oral interview and mathematical calculations or manipulation of materials).

**Description:** Learners will complete a series of short responses where they will employ a range of mathematical techniques and procedures, problem solving strategies and mathematical reasoning to make informed choices relating to personal situations involving measurement and geometry.

Evidence of mathematical thinking and calculations can be captured through observation and/or recording of use of manipulatives and learner responses and discussion can be captured through written, oral or AAC methods as appropriate for the learner. Additionally, where possible, learners

should be provided with opportunities to collaborate in pairs, or small groups and enabled to engage in mathematical discussion to share ideas, solutions and thinking.

**Size:** Between 6 and 10 responses equivalent to 2-3 written sentences each and associated mathematical calculations.

**Timing:** Ongoing throughout module.

**External agencies:** At teacher discretion.

**Relevant criteria:**

- Criterion 1: E1, E2, E3, E5 and where relevant E4
- Criterion 2: E1, E2, E3, E4 and E5 as appropriate
- Criterion 3: E1, E2 and where relevant E3
- Criterion 4: all elements
- Criterion 5: E1, E2, E3 and where relevant E4
- Criterion 7: all elements

### Module 3 Work Requirements Specifications

**Focus Area:** Personal Futures

**Title of Work Requirement:** Data Collection and Analysis Project

**Mode /Format:** Project

**Description:** Learners will complete a data collection and analysis project where they will employ a range of mathematical techniques and procedures, problem solving strategies and mathematical reasoning to make informed choices relating to personal situations involving probability and statistics.

Evidence of data collection, organisation and representation can be captured through observation and/or recording of use of manipulatives and learner responses and discussion can be captured through written, oral or AAC methods as appropriate for the learner. Additionally, where possible, learners should be provided with opportunities to collaborate in pairs, or small groups and enabled to engage in mathematical discussion to discuss their data collection process and results.

**Size:** Equivalent to 300 words in format appropriate to the learner.

**Timing:** Ongoing throughout module.

**External agencies:** At teacher discretion.

**Relevant criteria:**

- Criterion 1: E1, E2, E3, E5 and where relevant E4
- Criterion 2: E1, E2, E3, E4 and E5 as appropriate
- Criterion 3: E1, E2 and where relevant E3
- Criterion 4: all elements
- Criterion 5: E1, E2, E3 and where relevant E4
- Criterion 8: all elements

## Appendix 4 – General Capabilities and Cross-Curriculum Priorities

Learning across the curriculum content, including the cross-curriculum priorities and general capabilities, assists students to achieve the broad learning outcomes defined in the *Alice Springs (Mparntwe) Education Declaration (December 2019)*.

General Capabilities:

The general capabilities play a significant role in the Australian Curriculum in equipping young Australians to live and work successfully in the twenty-first century.

In the Australian Curriculum, capability encompasses knowledge, skills, behaviours and dispositions. Students develop capability when they apply knowledge and skills confidently, effectively and appropriately in complex and changing circumstances, in their learning at school and in their lives outside school.

The general capabilities include:

- Critical and creative thinking 
- Ethical understanding 
- Information and communication technology capability 
- Intercultural understanding 
- Literacy 
- Numeracy 
- Personal and social capability 

Cross-Curriculum Priorities:

Cross-curriculum priorities enable students to develop understanding about and address the contemporary issues they face, for their own benefit and for the benefit of Australia as a whole. The priorities provide national, regional and global dimensions which will enrich the curriculum through development of considered and focused content that fits naturally within learning areas. Incorporation of the priorities will encourage conversations between students, teachers and the wider community.

The cross-curriculum priorities include:

- Aboriginal and Torres Strait Islander Histories and Cultures 
- Asia and Australia's Engagement with Asia 
- Sustainability 

## Appendix 5 – Glossary

Term	Definition	Source Acknowledgement	Course Context
<b>algorithm</b>	An algorithm is a precisely defined routine procedure that can be applied and systematically followed through to a conclusion.	ACARA	Essential Mathematics I
<b>Associative operations</b>	<p>Operations are associative if the order in which operations take place does not affect the result.</p> <p>For example, addition of numbers is associative, since the order in which they are added does not change their sum. The corresponding associative law is:  <math>(a + b) + c = a + (b + c)</math> for all numbers <math>a</math>, <math>b</math> and <math>c</math>.</p> <p>Multiplication is also associative, as the product of the numbers does not vary with the order of their multiplication. The corresponding associative law is:  <math>(ab)c = a(bc)</math> for all numbers <math>a</math>, <math>b</math> and <math>c</math>.</p> <p>Subtraction and division are not associative, as the order of operations changes the value of the expression.</p>	ACARA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module I – Number and place value</li> </ul>
<b>calculates</b>	Determine or find (eg a number, answer) by using mathematical processes; obtain a numerical answer showing the relevant stages in the working; ascertain/determine from given facts, figures or information.	QCAA	Essential Mathematics I

Term	Definition	Source Acknowledgement	Course Context
<b>Cartesian plane</b>	<p>Two intersecting number lines are taken intersecting at right angles at their origins to form the axes of the coordinate system; the plane is divided into four quadrants by these perpendicular axes, called the x-axis (horizontal line) and the y-axis (vertical line); the position of any point in the plane can be represented by an ordered pair of numbers (x, y); these ordered pairs are called the coordinates of the point; this is called the Cartesian coordinate system; the plane is called the Cartesian plane.</p>	QCAA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 3 – Shapes, maps and plans</li> </ul>
<b>commutative operations</b>	<p>Operations are commutative if the order in which terms are given does not affect the result.</p> <p>The commutative law for addition is:</p> <p><math>a + b = b + a</math>, for all numbers <math>a</math> and <math>b</math>.</p> <p>For example, <math>3+5=5+3</math>.</p> <p>The commutative law for multiplication is: <math>ab = ba</math>, for all numbers <math>a</math> and <math>b</math>.</p> <p>For example, <math>4 \times 7 = 7 \times 4</math>.</p> <p>Subtraction and division are not commutative because for example <math>5-3 \neq 3-5</math> and <math>12 \div 4 \neq 4 \div 12</math>.</p>	ACARA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 1 – Number and place value</li> </ul>

Term	Definition	Source Acknowledgement	Course Context
<b>distributive law</b>	<p>Multiplication of numbers is said to be ‘distributive over addition’, because the product of one number with the sum of two others equals the sum of the products of the first number with each of the others.</p> <p>For example: the product of 3 with (4+5) gives the same result as the sum of <math>3 \times 4</math> and <math>3 \times 5</math>:</p> $3 \times (4+5) = 3 \times 9 = 27 \text{ and } 3 \times 4 + 3 \times 5 = 12 + 15 = 27$ <p>This distributive law is expressed algebraically as follows:  <math>a(b + c) = ab + ac</math>, for all numbers <math>a</math>, <math>b</math> and <math>c</math>.</p>	ACARA	<p>Essential Mathematics I:</p> <ul style="list-style-type: none"> <li>Module 1 – Number and place value</li> </ul>
<b>equivalence</b>	Two expressions are said to be equivalent if they are equal in value.		<p>Essential Mathematics I:</p> <ul style="list-style-type: none"> <li>Module 1 – Number and place value</li> </ul>
<b>face (shape)</b>	Any of the individual flat surfaces of a solid object.	mathsisfun.com	<p>Essential Mathematics I:</p> <ul style="list-style-type: none"> <li>Module 3 – Shapes, maps and plans</li> </ul>
<b>integer</b>	The integers are the “whole numbers” including those with negative sign $\dots -3, -2, -1, 0, 1, 2, 3 \dots$ . In Latin, the word integer means “whole.” The set of integers is usually denoted by $Z$ . Integers are basic building blocks in mathematics.	ACARA	<p>Essential Mathematics I:</p> <ul style="list-style-type: none"> <li>Module 1 – Number and place value</li> </ul>

Term	Definition	Source Acknowledgement	Course Context
<b>mean</b>	The arithmetic mean, $\bar{x}$ , of a list of numbers is the sum of the data values divided by the number of values in the list.  In everyday language, the arithmetic mean is commonly called the average.	ACARA	Essential Mathematics 1:  <ul style="list-style-type: none"> <li>Module 2 – Data collection, representation and interpretation</li> </ul>
<b>median</b>	The median is the value in a set of ordered set of data values that divides the data into two parts of equal size. When there are an odd number of data values, the median is the middle value. When there is an even number of data values, the median is the arithmetic mean of the two central values.	ACARA	Essential Mathematics 1:  <ul style="list-style-type: none"> <li>Module 2 – Data collection, representation and interpretation</li> </ul>
<b>mode</b>	The mode is the most frequently occurring value in a data set.	ACARA	Essential Mathematics 1:  <ul style="list-style-type: none"> <li>Module 2 – Data collection, representation and interpretation</li> </ul>
<b>order of operations</b>	The order of performing mathematical operations:  <ol style="list-style-type: none"> <li>1. evaluate brackets or grouping symbols first</li> <li>2. evaluate any powers and roots</li> <li>3. working left to right, evaluate any multiplication and division</li> <li>4. working left to right, evaluate any addition or subtraction (may also be known as BODMAS, BIDMAS, BEDMAS, etc).</li> </ol>	QCAA	Essential Mathematics 1
<b>partitioning</b>	Partitioning means dividing a quantity into parts. In the early years, it commonly refers to the ability to think about numbers as made up of two parts, such as, 10 is 8 and 2. In later years it refers to dividing both continuous and discrete quantities into equal parts.	ACARA	Essential Mathematics 1:  <ul style="list-style-type: none"> <li>Module 1 – Number and place value</li> </ul>

Term	Definition	Source Acknowledgement	Course Context
<b>picture graph</b>	A picture graph is a statistical graph for organising and displaying categorical data.	ACARA	Essential Mathematics 1: <ul style="list-style-type: none"> <li>Module 2 – Data collection, representation and interpretation</li> </ul>
<b>place value</b>	Place value refers to the value of a digit as determined by its position in a number, relative to the ones (or units) place. For integers, the ones place is occupied by the rightmost digit in the number. The value of the next column (the first after the decimal point) represents tenths of ones and this continues with the value of each corresponding digit being representative of a value 10 times smaller than the previous.  For example, in the number 2 594.6 the 4 denotes 4 ones, the 9 denotes 90 ones or 9 tens, the 5 denotes 500 ones or 5 hundreds, the 2 denotes 2000 ones or 2 thousands, and the 6 denotes $\frac{6}{10}$ of a one or 6 tenths.	ACARA	Essential Mathematics 1: <ul style="list-style-type: none"> <li>Module 1 – Number and place value</li> </ul>
<b>probability</b>	The likelihood or chance of something; the relative frequency of the occurrence of an event as measured by the ratio of the number of cases or alternatives favourable to the event to the total number of cases or alternatives.	QCAA	Essential Mathematics 1: <ul style="list-style-type: none"> <li>Module 2 – Chance</li> </ul>
<b>range</b>	The range is the difference between the largest and smallest observations in a data set.	ACARA	Essential Mathematics 1: <ul style="list-style-type: none"> <li>Module 2 – Data collection, representation and interpretation</li> </ul>

Term	Definition	Source Acknowledgement	Course Context
<b>rate</b>	A particular kind of ratio in which the two quantities are measured in different units; for example, the ratio of distance to time, known as speed, is a rate because distance and time are measured in different units (such as kilometres and hours); the value of the rate depends on the units in which the quantities are expressed.	QCAA	Essential Mathematics I
<b>ratio</b>	A comparison of two quantities of the same kind; for example, if a recipe uses 2 cups of milk and 3 cups of flour, the ratio of milk to flour is 2 is to 3. This can also be written with a colon, 2:3, or as a fraction, $\frac{2}{3}$ .	QCAA	Essential Mathematics I
<b>recurring decimal</b>	Non-terminating decimals may be recurring, that is, contain a pattern of digits that repeats indefinitely after a certain number of places.	ACARA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 1 – Fractions, decimals and percentages</li> </ul>
<b>reflection</b>	To reflect the point $A$ in an axis of reflection, a line is drawn at right angles to the axis of reflection and the point $A'$ is marked at the same distance from the axis of reflection as $A$ , but on the other side.  The point $A'$ is called the reflection image of $A$ .  A reflection is a transformation that moves each point to its reflection image.	ACARA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 3 – Geometric reasoning</li> </ul>
<b>sample</b>	Part of a population; a subset of the population, often randomly selected for the purpose of estimating the value of a characteristic of the population as a whole.	QCAA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 2 – Data collection, representation and interpretation</li> </ul>

Term	Definition	Source Acknowledgement	Course Context
<b>sample space</b>	The sample space of a chance experiment is the set of all possible outcomes for that experiment.	NESA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 2 – Chance</li> </ul>
<b>sampling</b>	<p>Sampling is the selection of a subset of data from a statistical population. Methods of sampling include:</p> <ol style="list-style-type: none"> <li>1. systematic sampling - sample data is selected from a random starting point and using a fixed periodic interval</li> <li>2. self-selecting sampling - non-probability sampling where individuals volunteer themselves to be part of a sample</li> <li>3. simple random sampling - sample data is chosen at random where each member has an equal probability of being chosen</li> <li>4. stratified sampling - after dividing the population into separate groups or strata, a random sample is then taken from each group/strata in an equivalent proportion to the size of that group/strata in the population.</li> </ol> <p>A sample can be used to estimate the characteristics of the statistical population.</p>	NESA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 2 – Data collection, representation and interpretation</li> </ul>
<b>scale</b>	A graduated line, as on a map, representing proportionate size.	QCAA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 3 – Shapes, maps and plans</li> </ul>
<b>sketch</b>	Execute a drawing or painting in simple form, giving essential features but not necessarily with detail or accuracy; in mathematics, represent by means of a diagram or graph; the sketch should give a general idea of the required shape or relationship and should include features.	QCAA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 3 – Shapes, maps and plans</li> </ul>

Term	Definition	Source Acknowledgement	Course Context
<b>symmetry</b>	<p>A plane figure <math>f</math> has line symmetry in a line <math>m</math>, if the image of <math>f</math> under the reflection in <math>m</math> is <math>f</math> itself. The line <math>m</math> is called the axis of symmetry.</p> <p>A plane figure <math>f</math> has rotational symmetry about a point <math>O</math> if there is a rotation such that the image of <math>f</math> under the rotation is <math>f</math> itself.</p>	ACARA	Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 3 – Geometric reasoning</li> </ul>
<b>terminating decimal</b>	A terminating decimal is a decimal that contains a finite number of digits.		Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 1 – Fractions, decimals and percentages</li> </ul>
<b>translation</b>	<p>Shifting a figure in the plane without turning it is called translation. To describe a translation in the plane, it is enough to say how far left or right and how far up or down the figure is moved.</p> <p>A translation is a transformation that moves each point to its translation image.</p>		Essential Mathematics I: <ul style="list-style-type: none"> <li>Module 3 – Geometric reasoning</li> </ul>

## Appendix 6 – Degree of difficulty of problems

Within this course, the degree of difficulty of problems a learner can answer correctly is a defining feature of their understanding. Within the criteria and standards, the expected depth of knowledge is described using the following terms.

### Simple familiar

Problems of this degree of difficulty require students to demonstrate knowledge and understanding of the subject matter and application of skills in a situation where:

- relationships and interactions are obvious and have few elements; and
- all of the information to solve the problem is identifiable; that is
  - the required procedure is clear from the way the problem is posed, or
  - in a context that has been a focus of prior learning.

### Complex familiar

Problems of this degree of difficulty require students to demonstrate knowledge and understanding of the subject matter and application of skills in a situation where:

- relationships and interactions have a number of elements, such that connections are made with subject matter within and/or across the domains of mathematics; and
- all of the information to solve the problem is identifiable; that is
  - the required procedure is clear from the way the problem is posed, or -
  - in a context that has been a focus of prior learning.

Some interpretation, clarification and analysis will be required to develop responses.

### Complex unfamiliar

Problems of this degree of difficulty require students to demonstrate knowledge and understanding of the subject matter and application of skills in a situation where:

- relationships and interactions have a number of elements, such that connections are made with subject matter within and/or across the domains of mathematics; and
- all the information to solve the problem is not immediately identifiable; that is
  - the required procedure is not clear from the way the problem is posed, and
  - in a context in which students have had limited prior experience.

Students interpret, clarify and analyse problems to develop responses.